Package 'Pade'

June 19, 2024

Type Package	
Title Padé Approximant Coefficients	
Version 1.0.7	
Date 2024-06-19	
Description Given a vector of Taylor series coefficients of sufficient length as input, the function returns the numerator and denominator coefficients for the Padé approximant of appropriate order (Baker, 1975) <isbn:9780120748556>.</isbn:9780120748556>	
License GPL (>= 2) BSD_2_clause + file LICENSE	
Imports utils	
Suggests covr, tinytest	
<pre>URL https://github.com/aadler/Pade</pre>	
BugReports https://github.com/aadler/Pade/issues	
Encoding UTF-8	
NeedsCompilation no	
Author Avraham Adler [aut, cph, cre] (https://orcid.org/0000-0002-3039-0703)	
Maintainer Avraham Adler <avraham.adler@gmail.com></avraham.adler@gmail.com>	
Repository CRAN	
Date/Publication 2024-06-19 21:40:10 UTC	
Contents	
Pade-package Pade	2 3
Index	5

2 Pade-package

kage Padé Approximant Coefficients

Description

Given a vector of Taylor series coefficients of sufficient length as input, the function returns the numerator and denominator coefficients for the Padé approximant of appropriate order (Baker, 1975) <ISBN:9780120748556>.

Details

The DESCRIPTION file:

Package: Pade Type: Package

Title: Padé Approximant Coefficients

Version: 1.0.7 Date: 2024-06-19

Authors@R: c(person(given="Avraham", family="Adler", role=c("aut", "cph", "cre"), email="Avraham.Adler@gmailer.com.adler@gmailer.com.adler@gmailer.com.adler

Description: Given a vector of Taylor series coefficients of sufficient length as input, the function returns the numeral

License: GPL (>= 2) | BSD_2_clause + file LICENSE

Imports: utils

Suggests: covr, tinytest

URL: https://github.com/aadler/Pade
BugReports: https://github.com/aadler/Pade/issues

Encoding: UTF-8 NeedsCompilation: no

Author: Avraham Adler [aut, cph, cre] (https://orcid.org/0000-0002-3039-0703)

Maintainer: Avraham Adler < Avraham. Adler @ gmail.com>

Index of help topics:

Pade Padé Approximant Coefficients
Pade-package Padé Approximant Coefficients

Author(s)

Avraham Adler [aut, cph, cre] (https://orcid.org/0000-0002-3039-0703)

Maintainer: Avraham Adler < Avraham. Adler @gmail.com>

Pade 3

Pade

Padé Approximant Coefficients

Description

Given Taylor series coefficients a_n from n=0 up to n=T, the function will calculate the Padé [L/M] approximant coefficients so long as $L+M \leq T$.

Usage

Pade(L, M, A)

Arguments

L Order of Padé numerator

M Order of Padé denominator

A vector of Taylor series coefficients, starting at x^0

Details

As the Taylor series expansion is the "best" polynomial approximation to a function, the Padé approximants are the "best" rational function approximations to the original function. The Padé approximant often has a wider radius of convergence than the corresponding Taylor series, and can even converge where the Taylor series does not. This makes it very suitable for computer-based numerical analysis.

The [L/M] Padé approximant to a Taylor series A(x) is the quotient

$$\frac{P_L(x)}{Q_M(x)}$$

where $P_L(x)$ is of order L and $Q_M(x)$ is of order M. In this case:

$$A(x) - \frac{P_L(x)}{Q_M(x)} = \mathcal{O}\left(x^{L+M+1}\right)$$

When q_0 is defined to be 1, there is a unique solution to the system of linear equations which can be used to calculate the coefficients.

The function accepts a vector A of length T + 1, composed of the a_n of the of truncated Taylor series

$$A(x) = \sum_{j=0}^{T} a_j x^j$$

and returns a list of two elements, Px and Qx, the Padé numerator and denominator coefficients respectively, as long as $L+M \leq T$.

4 Pade

Value

Pade returns a list with two entries:

Px Coefficients of the numerator polynomial starting at x^0 .

Qx Coefficients of the denominator polynomial starting at x^0 .

Author(s)

Avraham Adler < Avraham. Adler@gmail.com>

References

Baker, George Allen (1975) Essentials of Padé Approximants Academic Press. ISBN 978-0-120-74855-6

See Also

This package provides similar functionality to the pade function in the **pracma** package. However, it does not allow computation of coefficients beyond the supplied Taylor coefficients and it expects its input and provides its output in ascending—instead of descending—order.

See the **minimaxApprox** package for polynomial and rational minimax approximations to functions.

Examples

Index

```
* NumericalMathematics
Pade, 3
Pade-package, 2

* package
Pade-package, 2

Pade, 3

Pade-package, 2
```