mkin - Routines for fitting kinetic models with one or more state variables to chemical degradation data

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Abstract

In the regulatory evaluation of chemical substances like plant protection products (pesticides), biocides and other chemicals, degradation data play an important role. For the evaluation of pesticide degradation experiments, detailed guidance has been developed, based on nonlinear optimisation. The R add-on package **mkin** implements fitting some of the models recommended in this guidance from within R and calculates some statistical measures for data series within one or more compartments, for parent and metabolites.

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Key words: Kinetics, FOCUS, nonlinear optimisation

1 Introduction

Many approaches are possible regarding the evaluation of chemical degradation data. The **kinfit** package (Ranke, 2010a) in R (R Development Core Team, 2010) implements the approach recommended in the kinetics report provided by the FOrum for Co-ordination of pesticide fate models and their USe (FOCUS Work Group on Degradation Kinetics, 2006) for simple data series for one parent compound in one compartment.

The **mkin** package (Ranke, 2010b) extends this approach to data series with metabolites and more than one compartment and includes the possibility for back reactions.

2 Example

In the following, requirements for data formatting are explained. Then the procedure for fitting the four kinetic models recommended by the FOCUS group to an example dataset for parent only given in the FOCUS kinetics report is illustrated. The explanations are kept rather verbose in order to lower the barrier for R newcomers.

2.1 Data format

The following listing shows example dataset C from the FOCUS kinetics report as distributed with the **kinfit** package

```
R> library("mkin")
R> FOCUS_2006_C
```

```
    name time value
1 parent    0  85.1
2 parent    1  57.9
3 parent    3  29.9
```

```
4 parent    7  14.6
5 parent   14   9.7
6 parent   28   6.6
7 parent   63   4.0
8 parent   91   3.9
9 parent  119   0.6
```

Note that the data needs to be in the format of a data frame containing a variable `name` specifying the observed variable, indicating the compound name and, if applicable, the compartment, a variable `time` containing sampling times, and a numeric variable `value` specifying the observed value of the variable. If a further variable `error` is present, this will be used to give different weights to the data points (the higher the error, the lower the weight, see the help page of the `modCost` function of the **FME** package (Soetaert and Petzoldt, 2010)). Replicate measurements are not recorded in extra columns but simply appended, leading to multiple occurrences of the sampling times `time`.

Small to medium size dataset can be conveniently entered directly as R code as shown in the following listing

```
R> example_data <- data.frame(
+   time = c(0, 1, 3, 7, 14, 28, 63, 91, 119),
+   parent = c(85.1, 57.9, 29.9, 14.6, 9.7, 6.6, 4, 3.9, 0.6)
+ )
```

2.2 Model definition

The next task is to define the model to be fitted to the data. In order to facilitate this task, a convenience function `mkinmod` is available.

```
R> SFO <- mkinmod(parent = list(type = "SFO"))
R> SFORB <- mkinmod(parent = list(type = "SFORB"))
R> SFO_SFO <- mkinmod(
+   parent = list(type = "SFO", to = "m1", sink = TRUE),
+   m1 = list(type = "SFO"))
R> SFORB_SFO <- mkinmod(
+   parent = list(type = "SFORB", to = "m1", sink = TRUE),
+   m1 = list(type = "SFO"))
```

2.3 Fitting the model

Then the model parameters should be fitted to the data. The function `mkinfit` internally creates a cost function using `modCost` from the **FME** package and the produces a fit using `modFit` from the same package.

```
R> # Do not show significance stars as they interfere with vignette generation
R> options(show.signif.stars = FALSE)
R> SFO.fit <- mkinfit(SFO, FOCUS_2006_C)
```

```
Model cost at call  1 :  4718.97
Model cost at call  4 :  4718.97
Model cost at call  5 :  572.411
Model cost at call  7 :  572.4109
Model cost at call  8 :  236.2074
Model cost at call  9 :  236.2073
Model cost at call  11 :  198.936
Model cost at call  12 :  198.936
Model cost at call  14 :  196.6777
Model cost at call  15 :  196.6777
Model cost at call  16 :  196.6777
Model cost at call  17 :  196.5422
Model cost at call  18 :  196.5422
Model cost at call  19 :  196.5422
Model cost at call  20 :  196.5341
Model cost at call  21 :  196.5341
Model cost at call  22 :  196.5341
Model cost at call  23 :  196.5336
Model cost at call  25 :  196.5336
Model cost at call  26 :  196.5336
Model cost at call  28 :  196.5336
Model cost at call  29 :  196.5336
Model cost at call  33 :  196.5336
```

```
R> summary(SFO.fit)
```

```
Equations:
[1] d_parent = - k_parent_sink * parent

Starting values for optimised parameters:
              initial   type lower upper
parent_0        100.0  state     0   Inf
k_parent_sink     0.1 deparm     0   Inf

Fixed parameter values:
None

Optimised parameters:
              Estimate Std. Error t value Pr(>|t|)
parent_0       82.4919     4.7402  17.402 5.09e-07
k_parent_sink   0.3061     0.0459   6.668 0.000286

Residual standard error: 5.299 on 7 degrees of freedom

Chi2 error levels in percent:
```

```
          err.min n.optim df
All data   15.84       2  7
parent     15.84       2  7

Estimated disappearance times
        DT50  DT90
parent 2.265 7.523

Estimated formation fractions
            ff
parent_sink  1

Data:
 time variable observed       predicted residual
    0   parent     85.1 82.491909127670    2.608
    1   parent     57.9 60.742414863088   -2.842
    3   parent     29.9 32.934543136533   -3.035
    7   parent     14.6  9.682183711304    4.918
   14   parent      9.7  1.136405834674    8.564
   28   parent      6.6  0.015654973995    6.584
   63   parent      4.0  0.000000361301    4.000
   91   parent      3.9 -0.000000014466    3.900
  119   parent      0.6 -0.000000001821    0.600
```

```
R> SFORB.fit <- mkinfit(SFORB, FOCUS_2006_C)
```

```
Model cost at call  1 :  7044.136
Model cost at call  4 :  7044.136
Model cost at call  7 :  3460.144
Model cost at call  9 :  3460.144
Model cost at call  11 :  3460.144
Model cost at call  13 :  312.9751
Model cost at call  15 :  312.9750
Model cost at call  17 :  312.9750
Model cost at call  18 :  27.14491
Model cost at call  20 :  27.14491
Model cost at call  23 :  4.437647
Model cost at call  25 :  4.437646
Model cost at call  28 :  4.362915
Model cost at call  31 :  4.362915
Model cost at call  33 :  4.362711
Model cost at call  38 :  4.36271
Model cost at call  40 :  4.36271
Model cost at call  41 :  4.36271
Model cost at call  43 :  4.36271
Model cost at call  52 :  4.36271
```

```
R> summary(SFORB.fit)
```

```
Equations:
[1] d_parent_free = - k_parent_free_sink * parent_free - k_parent_free_bound * parent_fr
[2] d_parent_bound = + k_parent_free_bound * parent_free - k_parent_bound_free * parent_

Starting values for optimised parameters:
                    initial   type lower upper
parent_free_0         100.0  state     0   Inf
k_parent_free_sink      0.1 deparm     0   Inf
k_parent_free_bound     0.1 deparm     0   Inf
k_parent_bound_free     0.1 deparm     0   Inf

Fixed parameter values:
             value  type
parent_bound     0 state

Optimised parameters:
                     Estimate Std. Error t value Pr(>|t|)
parent_free_0       85.002757   0.890671  95.437 2.39e-09
k_parent_free_sink   0.395045   0.014308  27.610 1.17e-06
k_parent_free_bound  0.061599   0.007289   8.451 0.000381
k_parent_bound_free  0.020764   0.003752   5.533 0.002644

Residual standard error: 0.9341 on 5 degrees of freedom

Chi2 error levels in percent:
         err.min n.optim df
All data   2.662       4  5
parent     2.662       4  5

Estimated disappearance times
        DT50  DT90
parent 1.887 21.25

Estimated formation fractions
                 ff
parent_free_sink  1

Data:
 time variable observed predicted residual
    0   parent     85.1    85.003  0.09724
    1   parent     57.9    58.039 -0.13907
    3   parent     29.9    30.054 -0.15353
    7   parent     14.6    13.866  0.73384
   14   parent      9.7     9.787 -0.08661
   28   parent      6.6     7.532 -0.93204
   63   parent      4.0     4.033 -0.03263
   91   parent      3.9     2.446  1.45354
  119   parent      0.6     1.484 -0.88418
```

```
R> SFO_SFO.fit <- mkinfit(SFO_SFO, FOCUS_2006_D)

Model cost at call  1 :  18994.29
Model cost at call  3 :  18994.29
Model cost at call  7 :  10641.39
Model cost at call  8 :  10641.39
Model cost at call  12 :  7145.411
Model cost at call  14 :  7145.41
Model cost at call  17 :  411.9753
Model cost at call  18 :  411.9751
Model cost at call  22 :  371.2194
Model cost at call  23 :  371.2194
Model cost at call  27 :  371.2127
Model cost at call  31 :  371.2127
Model cost at call  32 :  371.2127
Model cost at call  37 :  371.2127
Model cost at call  39 :  371.2127
Model cost at call  41 :  371.2127
Model cost at call  45 :  371.2127

R> summary(SFO_SFO.fit)

Equations:
[1] d_parent = - k_parent_sink * parent - k_parent_m1 * parent
[2] d_m1 = - k_m1_sink * m1 + k_parent_m1 * parent

Starting values for optimised parameters:
              initial   type lower upper
parent_0        100.0  state     0   Inf
k_parent_sink     0.1 deparm     0   Inf
k_m1_sink         0.1 deparm     0   Inf
k_parent_m1       0.1 deparm     0   Inf

Fixed parameter values:
   value  type
m1     0 state

Optimised parameters:
               Estimate Std. Error t value Pr(>|t|)
parent_0      9.960e+01  1.614e+00  61.720  < 2e-16
k_parent_sink 4.792e-02  3.750e-03  12.778 6.10e-15
k_m1_sink     5.261e-03  7.159e-04   7.349 1.15e-08
k_parent_m1   5.078e-02  2.094e-03  24.248  < 2e-16

Residual standard error: 3.211 on 36 degrees of freedom

Chi2 error levels in percent:
         err.min n.optim df
All data   6.565       4 16
parent     6.827       3  6
```

```
m1         4.748       1 10

Estimated disappearance times
          DT50   DT90
parent   7.023  23.33
m1     131.761 437.70

Estimated formation fractions
                ff
parent_sink 0.4855
parent_m1   0.5145
m1_sink     1.0000

Data:
 time variable observed  predicted    residual
    0   parent    99.46 99.5984780  -0.1384780
    0   parent   102.04 99.5984780   2.4415220
    1   parent    93.50 90.2378698   3.2621302
    1   parent    92.50 90.2378698   2.2621302
    3   parent    63.23 74.0731862 -10.8431862
    3   parent    68.99 74.0731862  -5.0831862
    7   parent    52.32 49.9120818   2.4079182
    7   parent    55.13 49.9120818   5.2179182
   14   parent    27.27 25.0126181   2.2573819
   14   parent    26.64 25.0126181   1.6273819
   21   parent    11.50 12.5346278  -1.0346278
   21   parent    11.64 12.5346278  -0.8946278
   35   parent     2.85  3.1478698  -0.2978698
   35   parent     2.91  3.1478698  -0.2378698
   50   parent     0.69  0.7162389  -0.0262389
   50   parent     0.63  0.7162389  -0.0862389
   75   parent     0.05  0.0607378  -0.0107378
   75   parent     0.06  0.0607378  -0.0007378
  100   parent       NA  0.0051507          NA
  100   parent       NA  0.0051507          NA
  120   parent       NA  0.0007155          NA
  120   parent       NA  0.0007155          NA
    0       m1     0.00  0.0000000   0.0000000
    0       m1     0.00  0.0000000   0.0000000
    1       m1     4.84  4.8029540   0.0370460
    1       m1     5.64  4.8029540   0.8370460
    3       m1    12.91 13.0239981  -0.1139981
    3       m1    12.96 13.0239981  -0.0639981
    7       m1    22.97 25.0447443  -2.0747443
    7       m1    24.47 25.0447443  -0.5747443
   14       m1    41.69 36.6899902   5.0000098
   14       m1    33.21 36.6899902  -3.4799902
   21       m1    44.37 41.6530844   2.7169156
   21       m1    46.44 41.6530844   4.7869156
```

```
 35       m1    41.22 43.3131175  -2.0931175
 35       m1    37.95 43.3131175  -5.3631175
 50       m1    41.19 41.2183136  -0.0283136
 50       m1    40.01 41.2183136  -1.2083136
 75       m1    40.09 36.4470397   3.6429603
 75       m1    33.85 36.4470397  -2.5970397
100       m1    31.04 31.9816345  -0.9416345
100       m1    33.13 31.9816345   1.1483655
120       m1    25.15 28.7898510  -3.6398510
120       m1    33.31 28.7898510   4.5201490
```

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