

A simple graph system - gRash

Søren Højsgaard

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1 Introduction

This is a technical note which describes a simple “graph system” in R called `gRash`. The system is used in the `gRain` package¹ for graphical independence networks. Thus `gRash` is not an R package but a part of an R package.

For the R community, the triplet triplet of the packages `graph`, `RBGL` and `Rgraphviz` consitutues tool for graph operations, manipulation and layout. The `gRash` system is not intended to be a strong competitor for these fine packages. On the contrary, part of the `gRash` functionality uses the other packages.

The main virtue of the `gRash` system is that graphs are specified in a way closer to normal text book representations and the same applies to some extent to the graph operations.

Only undirected and directed acyclic graphs are implemented.

2 Graphs

2.1 Undirected graphs

An undirected graph is created by the `newugsh` function. The graph can be specified by an incidence list in either of two different forms:

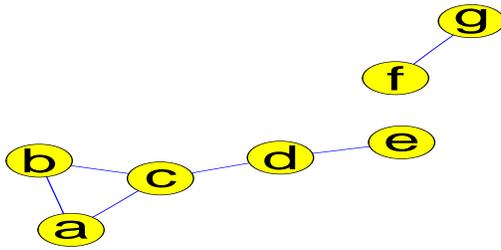
```
> ug1 <- newug(~a + b + c, ~c + d, ~d + e, ~f + g)
> ug1 <- newug(c("a", "b", "c"), c("c", "d"), c("d", "e"), c("f", "g"))
> ug1
```

```
Undirected graph
Nodes: a b c d e f g
Edges: a~b a~c b~c c~d d~e f~g
```

Graphs are displayed with `plot`:

```
> plot(ug1)
```

¹The package is not on CRAN but is available from <http://gbi.agrsci.dk/~shd/Public/gRainweb/>



2.2 Directed acyclic graphs

A directed acyclic graph can be specified as:

```

> dag1 <- newdag(~a, ~b + a, ~c + a, ~d + b + c, ~e + c)
> dag1 <- newdag("a", c("b", "a"), c("c", "a"), c("d", "b", "c"), c("e", "c"))
> dag1
  
```

```

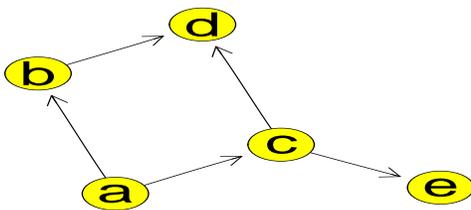
Directed graph
Nodes: a b c d e
Edges: b<-a c<-a d<-b d<-c e<-c
  
```

Here `~a` means that “a” has no parents while `~d+b+c` means that “d” has parents “b” and “c”.

Graphs are displayed with `plot`:

```

> plot(dag1)
  
```



3 Operations on undirected graphs

3.1 Graph queries

Many features of a graph are obtained by asking queries using the `queryg` function:

3.1.1 Nodes

```

> queryg(ug1, "nodes")
  
```

```

a b c d e f g
  
```

3.1.2 Edges

```
> queryg(ug1, "edges")
```

```
a b  
a c  
b c  
c d  
d e  
f g
```

3.1.3 Cliques

```
> queryg(ug1, "cliques")
```

```
c b a  
c d  
e d  
f g
```

3.1.4 Connected components

```
> queryg(ug1, "concomp")
```

```
a b c d e  
f g
```

3.1.5 Closure

```
> queryg(ug1, "cl", "c")
```

```
c a b d
```

3.1.6 Adjacencies

```
> queryg(ug1, "adj", "c")
```

```
a b d
```

3.1.7 Simplicial nodes

Nodes whose boundary is complete.

```
> queryg(ug1, "simplicialNodes")
```

```
a b e f g
```

3.1.8 Is complete

Is the graph complete?

```
> queryg(ug1, "is.complete")
```

```
[1] FALSE
```

3.1.9 Is simplicial

Is a node/set simplicial?

```
> queryg(ug1, "is.simplicial", "a")
```

```
[1] TRUE
```

```
> queryg(ug1, "is.simplicial", c("a", "b", "d"))
```

```
[1] FALSE
```

3.1.10 Is triangulated

```
> queryg(ug1, "is.triangulated")
```

```
[1] TRUE
```

3.1.11 Is A and B separated by S

```
> queryg(ug1, "separates", c("a", "b"), c("e", "f"), "d")
```

```
[1] TRUE
```

3.1.12 Subgraph

```
> queryg(ug1, "subgraph", c("a", "b", "c"))
```

```
Undirected graph  
Nodes: a b c  
Edges: c~b c~a b~a
```

3.2 Adjacency matrix

```
> convertg(ug1, to = "matrix")
```

```

      a   b   c   d   e   f   g
a FALSE TRUE TRUE FALSE FALSE FALSE FALSE
b TRUE  FALSE TRUE FALSE FALSE FALSE FALSE
c TRUE  TRUE  FALSE TRUE  FALSE FALSE FALSE
d FALSE FALSE TRUE  FALSE TRUE  FALSE FALSE
e FALSE FALSE FALSE  TRUE  FALSE FALSE FALSE
f FALSE FALSE FALSE  FALSE FALSE FALSE TRUE
g FALSE FALSE FALSE  FALSE FALSE TRUE  FALSE

```

3.3 Triangulation and Maximum Cardinality Search

3.3.1 Maximum cardinality search

Testing for whether a graph is triangulated is based on Maximum Cardinality Search:

```

> g <- newug(~a + b, ~b + c, ~c + d, ~d + e, ~e + a)
> mcs(g)

```

```

NULL

```

3.3.2 Triangulation

```

> tg <- triangulate(g)
> tg

```

```

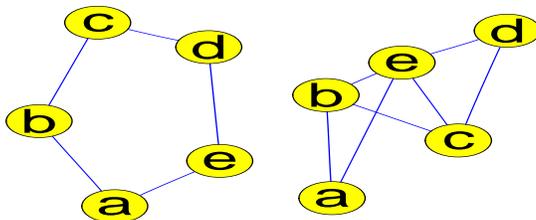
Undirected graph
Nodes: a b c d e
Edges: a~b b~c c~d a~e b~e c~e d~e

```

```

> par(mfrow = c(1, 2))
> plot(g)
> plot(tg)

```



3.3.3 RIP ordering of the cliques

A RIP ordering of the cliques of a triangulated graph:

```

> rip <- ripOrder(tg)
> names(rip)

```

```

nodes cliques separators pa nLevels ch

```

```
> rip
```

```
Cliques  
1 a b e  
2 b e c  
3 e c d  
Separators  
1 NA  
2 b e  
3 e c  
Parents  
1 NA  
2 1  
3 2
```

4 Operations on directed acyclic graphs

4.1 Graph queries

Many features of a graph are obtained by asking queries using the `queryg` function as above:

4.1.1 Parents

```
> queryg(dag1, "pa", "d")
```

```
b c
```

4.1.2 Children

```
> queryg(dag1, "ch", "c")
```

```
d e
```

4.1.3 Ancestral set

```
> queryg(dag1, "ancestralSet", c("b", "e"))
```

```
a b c e
```

4.2 Moralization

```
> moralize(dag1)
```

```
Undirected graph  
Nodes: a b c d e  
Edges: a~b a~c b~c b~d c~d c~e
```

4.3 Ancestral graph

```
> ancestralGraph(dag1, c("b", "e"))
```

```
Directed graph  
Nodes: a b c e  
Edges: e<-c c<-a b<-a
```

4.4 Checking for acyclicity

If a directed graph contains cycles, then NULL is returned

```
> newdag(~a + b, ~b + c, ~c + a)
```

```
NULL
```